## This and upcoming lectures?

- We'll focus on concepts relating to time
- Time as it can be "used" in systems
- Systems that present behaviors best understood in terms of temporal models (notably the transactional model)
- Event ordering used to ensure consistency in distributed systems (multicasts that update replicated data or program state)


## What time is it?

- In distributed system we need practical ways to deal with time
- E.g. we may need to agree that update A occurred before update B
- Or offer a "lease" on a resource that expires at time 10:10.0150
- Or guarantee that a time critical event will reach all interested parties within 100 ms


## But what does time "mean"?

- Time on a global clock?
- E.g. with GPS receiver
- ... or on a machine's local clock
- But was it set accurately?
- And could it drift, e.g. run fast or slow?
- What about faults, like stuck bits?
- ... or could try to agree on time


## Lamport's approach

- Leslie Lamport suggested that we should reduce time to its basics
- Time lets a system ask "Which came first: event A or event B?"
- In effect: time is a means of labeling events so that...
- If A happened before $B, \operatorname{TIME}(A)<\operatorname{TIME}(B)$
- If $\operatorname{TIME}(A)<\operatorname{TIME}(B), A$ happened before $B$


## Drawing time-line pictures:



- A, B, C and D are "events".
- Could be anything meaningful to the application
- So are snd(m) and $\operatorname{rcv}(m)$ and deliv(m)
- What ordering claims are meaningful?

Drawing time-line pictures:


- A happens before $B$, and $C$ before $D$
- "Local ordering" at a single process
- Write $\underset{A \rightarrow B}{p}$ and $C \xrightarrow{\eta} D$


## Drawing time-line pictures:



- $\operatorname{snd}_{p}(m)$ also happens before $r^{2}{ }_{q}(m)$
- "Distributed ordering" introduced by a message
- Write $\operatorname{snd}_{p}(m) \xrightarrow{n} r c_{q}(m)$


## Drawing time-line pictures:

## Drawing time-line pictures:

- A happens before D
- Transitivity: A happens before $\operatorname{snd}_{p}(m)$, which happens before $\operatorname{rcv}_{q}(m)$, which happens before $D$


## Happens before "relation"

- We'll say that "A happens before $B$ ", written $A \rightarrow B$, if

1. $A \rightarrow{ }^{P} B$ according to the local ordering, or
2. $A$ is a snd and $B$ is a rcv and $A \rightarrow{ }^{M} B$, or
3. $A$ and $B$ are related under the transitive closure of rules (1) and (2)

- So far, this is just a mathematical notation, not a "systems tool"

- B and D are concurrent
- Looks like B happens first, but D has no way to know. No information flowed...


## Logical clocks

- A simple tool that can capture parts of the happens before relation
- First version: uses just a single integer
- Designed for big (64-bit or more) counters
- Each process $p$ maintains $L T_{p,}$ a local counter
- A message $m$ will carry $L T_{m}$
- When an event happens at a process $p$ it increments $L T_{p}$.
- Any event that matters to $p$
- Normally, also snd and rcv events (since we want receive to occur "after" the matching send)
- When $p$ sends $m$, set
- $\mathrm{LT} \mathrm{T}_{\mathrm{m}}=\mathrm{LT} \mathrm{p}_{\mathrm{p}}$
- When q receives $m$, set
- $L T_{q}=\max \left(L T_{q}, L T_{m}\right)+1$


## Logical clocks

- If $A$ happens before $B, A \rightarrow B$, then $\operatorname{LT}(A)<L T(B)$
- But converse might not be true:
- If $\operatorname{LT}(A)<L T(B)$ can't be sure that $A \rightarrow B$
- This is because processes that don't communicate still assign timestamps and hence events will "seem" to have an order


## Vector clocks

## Time-line with VT annotations

- Clock is a vector: e.g. VT(A)=[1, 0]
- We'll just assign p index 0 and $q$ index 1
- Vector clocks require either agreement on the numbering, or that the actual process id's be included with the vector
- Rules for managing vector clock
- When event happens at p , increment $\mathrm{VT}_{\mathrm{p}}\left[\right.$ index ${ }_{p}$ ] - Normally, also increment for snd and rcv events
- When sending a message, set $\mathrm{VT}(\mathrm{m})=\mathrm{VT}_{\mathrm{p}}$
- When receiving, set $\mathrm{VT}_{\mathrm{q}}=\max \left(\mathrm{VT}_{\mathrm{q}}, \mathrm{VT}(\mathrm{m})\right)$


Could also be $[1,0]$ if we decide not to increment the clock on a snd event. Decision depends on how the timestamps will be used.

## Rules for comparison of VTs

- We'll say that $\mathrm{VT}_{\mathrm{A}} \leq \mathrm{VT}_{\mathrm{B}}$ if
- $\forall_{\mathrm{I}} \mathrm{VT}_{\mathrm{A}}[\mathrm{i}] \leq \mathrm{VT}_{\mathrm{B}}[\mathrm{i}]$
- And we'll say that $\mathrm{VT}_{\mathrm{A}}<\mathrm{VT}_{\mathrm{B}}$ if
$-\mathrm{VT}_{\mathrm{A}} \leq \mathrm{VT}_{\mathrm{B}}$ but $\mathrm{VT}_{\mathrm{A}} \neq \mathrm{V} \mathrm{T}_{\mathrm{B}}$
- That is, for some $\mathrm{i}, \mathrm{VT}_{\mathrm{A}}[\mathrm{i}]<\mathrm{VT}_{\mathrm{B}}[\mathrm{i}]$
- Examples?
- $[2,4] \leq[2,4]$
- $[1,3]<[7,3]$
- [1,3] is "incomparable" to [3,1]


## Time-line with VT annotations



- $\operatorname{VT}(A)=[1,0]$. $\operatorname{VT}(\mathrm{D})=[2,4]$. So $\mathrm{VT}(\mathrm{A})<\mathrm{VT}(\mathrm{D})$
- $\operatorname{VT}(\mathrm{B})=[3,0]$. So $\mathrm{VT}(\mathrm{B})$ and $\mathrm{VT}(\mathrm{D})$ are incomparable


## Vector time and happens before

- If $\mathrm{A} \rightarrow \mathrm{B}$, then $\mathrm{VT}(\mathrm{A})<\mathrm{VT}(\mathrm{B})$
- Write a chain of events from $A$ to $B$
- Step by step the vector clocks get larger
- If $\mathrm{VT}(\mathrm{A})<\mathrm{VT}(\mathrm{B})$ then $\mathrm{A} \rightarrow \mathrm{B}$
- Two cases: if $A$ and $B$ both happen at same process $p$, trivial
- If $A$ happens at $p$ and $B$ at $q$, can trace the path back by which $q$ "learned" $\mathrm{VT}_{A}[\mathrm{p}]$
- Otherwise A and B happened concurrently


## Synchronizing clocks

- Without help, clocks will often differ by many milliseconds
- Problem is that when a machine downloads time from a network clock it can't be sure what the delay was
- This is because the "uplink" and "downlink" delays are often very different in a network
- Outright failures of clocks are rare...


## Introducing "wall clock time"

- There are several options
- "Extend" a logical clock or vector clock with the clock time and use it to break ties
- Makes meaningful statements like "B and D were concurrent, although B occurred first"
- But unless clocks are closely synchronized such statements could be erroneous!
- We use a clock synchronization algorithm to reconcile differences between clocks on various computers in the network


## Synchronizing clocks



- Suppose p synchronizes with time. windows.com and notes that 123 ms elapsed while the protocol was running... what time is it now?


## Synchronizing clocks

- Options?
- $P$ could guess that the delay was evenly split, but this is rarely the case in WAN settings (downlink speeds are higher)
- P could ignore the delay
- P could factor in only "certain" delay, e.g. if we know that the link takes at least 5 ms in each direction. Works best with GPS time sources!
- In general can't do better than uncertainty in the link delay from the time source down to $p$


## Consequences?

- In a network of processes, we must assume that clocks are
- Not perfectly synchronized. Even GPS has uncertainty, although small
- We say that clocks are "inaccurate"
- And clocks can drift during periods between synchronizations
- Relative drift between clocks is their "precision"


## Thought question

- We are building an anti-missile system
- Radar tells the interceptor where it should be and what time to get there
- Do we want the radar and interceptor to be as accurate as possible, or as precise as possible?



## Thought question

- We want them to agree on the time but it isn't important whether they are accurate with respect to "true" time
- "Precision" matters more than "accuracy"
- Although for this, a GPS time source would be the way to go
- Might achieve higher precision than we can with an "internal" synchronization protocol!


## Real systems?

- Typically, some "master clock" owner periodically broadcasts the time
- Processes then update their clocks
- But they can drift between updates
- Hence we generally treat time as having fairly low accuracy
- Often precision will be poor compared to message round-trip times


## For next time

- Read the introduction to Chapter 14 to be sure you are comfortable with notions of time and with notation
- Chapter 23 looks at clock synchronization


## Clock synchronization

- To optimize for precision we can
- Set all clocks from a GPS source or some other time "broadcast" source
- Limited by uncertainty in downlink times
- Or run a protocol between the machines
- Many have been reported in the literature
- Precision limited by uncertainty in message delays
- Some can even overcome arbitrary failures in a subset of the machines!

